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ON THE DIFFERENCE BETWEEN OPTIMAL COMBINATION FUNCTIONS FOR VERIFICATION AND IDENTIFICATION SYSTEMS

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We have investigated different scenarios of combining pattern matchers. The combination problem can be viewed as a construction of a postprocessing classifier operating on the matching scores of the combined matchers. The optimal combination algorithm for verification systems corresponds to the likelihood ratio combination function. It can be implemented by the direct reconstruction of this function with genuine and impostor score density approximations. However, the optimal combination algorithm for identification systems is difficult to express analytically. We will show that this difficulty is caused by the dependencies between matching scores assigned to different classes by the same classifier. The experiments on the large sets of scores from handwritten word recognizers operating on postal images and biometric matchers (NIST biometric score set BSSR1) confirm the existence of such dependencies and that the optimal combination functions for verification and identification systems are different.

Keywords: Combination of classifiers; biometric identification systems; likelihood ratio; weighted sum.

1. Introduction

In this paper, we investigate the problem of combining the outputs of multiple classifiers. Combined classifiers might use different features or different matching algorithms, and as the large body of previous research shows, the combined algorithm can have superior performance when compared to any single participating classifier. We will assume that the set of classifiers being combined is fixed. Therefore we do not consider the problem of classifier ensembles with dynamically generated set of classifiers. In fact, in this study we will be only considering the combination of two given classifiers. Thus our problem consists of learning the statistical properties of each classifier's output and finding the proper combination algorithm.

We will also assume that each classifier outputs a numerical matching score for each class which reflects the confidence that the input belongs to that class. We will call such classifiers "matchers" to distinguish them from other types of classifiers

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1 which output only a single class label corresponding to the most probable class of the
 3 input or class ranks. Xu *et al.*²⁸ described three types of classifier combinations based
 on the types of output produced by a single participating classifier. In this paper, we
 5 deal with type III combinations which return a measurement level scores corre-
 sponding to every class which can be used to rank the classes.

7 The applications considered in this paper include the combination of multimodal
 biometric matchers and handwritten word recognizers. In both cases, two matchers
 9 process the input and produce an output consisting of two matching scores for each
 class. In the case of biometric matchers, the input consists of fingerprint and face
 11 templates, and the classes are the enrolled persons. The two matching fingerprint
 and face scores are used to obtain a single combined score for each person, and the
 13 person corresponding to the best combined score is output as the system's classifi-
 cation result. In case of handwritten word recognizers, the input is an image of a
 15 word, and the classes are the words in a lexicon. Two matchers are used to obtain two
 matching scores for each lexical entry. The combination algorithms produce a single
 17 combined score for each entry, and the lexical entry with best combined score is
 taken as the classification result.

19 **1.1. Problem description**

21 Let M denote the number of combined classifiers and N denote the number of classes.
 Each classifier $j = 1, \dots, M$ produces sets of matching scores s_i^j assigned to each of
 23 $i = 1, \dots, N$ classes. Our combination methods will operate on these scores. In both
 the biometric and word recognition applications, a combination function f of scores is
 25 used to combine M matching scores corresponding to each class, and the classifi-
 cation result C is determined by the corresponding combination rule:

$$27 \quad C = \arg \max_{i=1, \dots, N} f(s_i^1, \dots, s_i^M) \quad (1)$$

29 Note that the upper index of the score corresponds to the classifier which produced
 31 the score, and the lower index corresponds to the class for which it was produced.
 The sum function $f(s^1, \dots, s^M) = s^1 + \dots + s^M$ corresponds to the sum rule, the
 33 product function $f(s^1, \dots, s^M) = s^1 \dots s^M$ corresponds to the product rule and so
 on. Such combination functions commonly used by researchers are usually fixed (as
 35 opposed to being learned from training data).¹⁷ Using these fixed combination rules
 usually requires a processing step to normalize the matching scores. In general, these
 37 *ad hoc* functions are not optimal. We are interested in deriving the optimal combi-
 nation function f of Eq. (1) using training data and machine learning algorithms. We
 39 illustrate with the help of artificial examples the difficulty of this task even when a
 sufficient number of training samples are available.

41 The set of matching scores available for the combination algorithm is shown
 (Fig. 1) as a lattice with rows containing the scores produced by a classifier j and
 columns containing the scores assigned to a class i . The combination function f

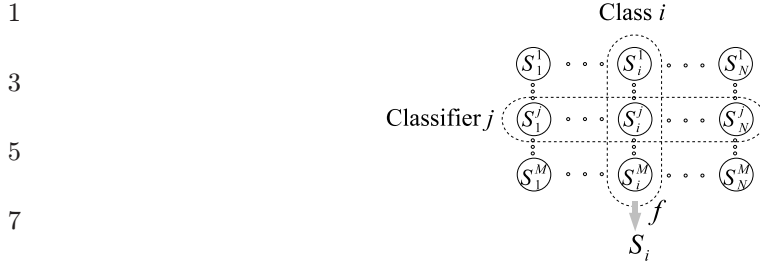


Fig. 1. The set of matching scores available for the combination algorithms in identification systems.

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accepts as parameters scores for class i (s_i^1, \dots, s_i^M) and produces a combined score S_i .

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1.2. Verification and identification modes

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Note, that two modes of operation are usually considered for the matching system. In the first, *verification* mode, the identity of the class i is provided as a hypothesis, and the decision to accept or reject class i as a matching result is based on comparing the combined score S_i to some threshold. In the second, *identification* mode, no hypothesis is provided and combined scores S_i are calculated for all classes i . The final classification decision is made by choosing the class with the greatest score returned by Eq. (1). *Our goal is to find the optimal combination function for the identification system.* The guiding intuition of our research is to compare the problem of finding the optimal combination function f of the identification system of Eq. (1) with the problem of finding the optimal combination function of the same system operating in the verification mode.

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Different modes of operation require different measures of performance. Whereas ROC or DET curves are useful for measuring performance in verification systems, the performance in identification systems is usually measured by the correct identification rate or cumulative match curve (CMC). In this paper, we use correct identification (classification) rate, that is the frequency of correctly identifying the class by Eq. (1).

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One very important notion that we explore in this paper is the notion of score dependence. Note, that there could be two types of score dependencies in a matching system (Fig. 1). The first type of dependence is that between matchers — between the scores assigned by different matchers to a single class. This is the dependence between scores in a column (s_i^1, \dots, s_i^M). The second type of dependence is that between scores produced by a single matcher and assigned to different classes. One can view it as a dependence between scores located in a single row (s_1^j, \dots, s_N^j). The first type of dependence has been the focus of researchers thus far and is adequately addressed in the construction of the combination function f . However, the main focus of our research in this paper is in the second type of dependence.

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1 Understanding this dependence is a necessary step in constructing optimal combi-
2 nation function for identification systems.

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5 **1.3. Paper outline**

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7 In the next section, we review some of the previous research in classifier combination
8 field. In Sec. 3, we show that the optimal combination function for verification
9 systems will be also optimal for equivalent identification systems only if an additional
10 condition of independence of matching scores assigned to different classes is satisfied.
11 Section 4 presents two important examples to illustrate that if this independence
12 condition is not satisfied, then the optimal combination functions of the two systems
13 are necessarily different. This is a fundamental finding in the classifier combination
14 field based on our assessment and literature review.

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16 Section 5 provides experiments confirming the difference in the optimal combi-
17 nation functions for verification and identification systems. First, we introduce the
18 handwritten word recognizers (Sec. 5.1) and biometric matchers (Sec. 5.2) which are
19 used in the experiments. The dependence between scores returned by a single
20 matcher for different classes is presented in Sec. 5.3. In Sec. 5.5, we compare the use
21 of likelihood ratio and weighted sum functions for combination.

22

23 **2. Previous Work**

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25 Although research in the classifier combination field has produced several new
26 combination algorithms, a theoretical underpinning for this research area is still
27 missing. Jain *et al.*¹⁵ stated that methods claiming optimality actually make rather
28 strict assumptions on the properties of the classifiers being combined. For example,
29 Kittler *et al.*¹⁷ assumed that the matching scores produced by the classifiers parti-
30 cipating in the combination correspond to posterior class probabilities, thus justi-
31 fying their use of product or sum combination rules depending on some additional
32 assumptions. In the applications we have considered in this paper, the matching
33 scores reflect distance measures between the biometric templates or between the
34 handwritten word image and a lexicon word. These distances can be converted to
35 probabilities,^{6,9,14} but this conversion is nontrivial and prone to errors.³

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37 Snelick *et al.*²⁰ investigated the combination of three fingerprint and one face
38 biometric matchers. Five combination methods and five score normalization func-
39 tions are tested to construct the combination algorithm. Since only a limited number
40 of combination algorithms are tested, there is no guarantee that the method finally
41 chosen is optimal or even close to optimal.

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43 Bayesian and Dempster-Shafer combination methods in Ref. 28 required learning
44 confusion matrices for each classifier participating in the combination. The Behavior-
45 Knowledge Space combination method in Ref. 13 requires learning a decision space of
46 a set of classifiers participating in the combination. Although these approaches can
47 be considered to be optimal in some sense, their utility is restricted to applications

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1 with a few classes. However, in our applications of biometrics and handwritten word
2 recognition, the number of classes N is of the order of thousands.

3 The goal of combination methods proposed in this paper is to perform combi-
4 nations in identification systems [Eq. (1)] with a large number of classes N . We show
5 that optimal combinations in identification and verification systems need not be the
6 same. Our primary interest is in approximating the optimal combination functions
7 for identification systems. Previous work in classifier combination has actually failed
8 to address this differentiation, and the performance of generic combination methods
9 has been evaluated without paying attention to whether they are designed for
10 identification systems or verification systems. For example, Lee *et al.*¹⁸ explicitly
11 reduced the problem of combining matchers in a biometric identification system to
12 the task of applying a classifier (SVM) trained for an equivalent verification system.
13 We show in this paper, by means of artificial examples (Sec. 4), that such an
14 approach may not produce an optimal combination algorithm for identification
15 systems.

16 Some researchers^{5,12} have tried to predict the performance of an identification
17 system given data about the performance of an equivalent verification system. The
18 necessary condition used in these predictions is the independence of matching
19 scores assigned to different classes. Our experiments show that this condition is
20 unrealistic and the scores are usually dependent. Therefore, the predictions of
21 performance of identification systems based on observations made in verification
22 systems might not be valid. In fact, the score dependence is precisely the reason
23 why verification and identification systems require different classifier combination
24 algorithms.

25 One way to account for the dependence of scores assigned to different classes is to
26 use not only single scores assigned to one class by combined classifiers, but some
27 additional information derived from scores assigned to other classes. Such infor-
28 mation might include the rank of the current score, the difference between this score
29 and the best assigned score, or any other statistic of the score set produced by the
30 same classifier. The combination methods based on ranks, e.g. Behavior-Knowledge
31 Space,¹³ might be efficient in using this information, but the original score gets
32 discarded. More complex schemes, such as in Ref. 2, consider the weighting of in-
33 formation (e.g. difference between scores) and can provide better performance than
34 combinations using ranks only. But, as we discussed in Ref. 22, such combinations
35 belong to more complex type of combinations not defined by Eq. (1). We restrict our
36 attention in the current paper to seeking proper combination functions of Eq. (1),
37 though investigating more complex combinations explicitly including the depen-
38 dence information should be one of future research directions.

39 We have presented the initial results of our investigation into the properties of
40 optimal combination functions in identification systems in Refs. 25 and 26. In this
41 paper, we provide a deeper discussion on the relationship between dependence of
42 matching scores and the construction of optimal combination function. In particular,

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1 two illustrative examples in Sec. 4 give an insight to the difficulty of finding the
 2 optimal combination function for identification systems.

3 **3. Likelihood Ratio Based Combination Rule**

4 In both applications of biometrics and handwriting recognition, we encounter ver-
 5 ification and identification modes of operation. We have already described in Sec. 1.2
 6 the two modes in the context of biometrics. The verification mode of operation occurs
 7 in handwriting recognition applications such as a bank check recognition system
 8 where the recognizers have to verify the hypothesis generated by the numeric string
 9 in the courtesy field.¹¹ The identification mode is precisely how handwritten word
 10 recognizers operate in postal applications where the task is to recognize the city and
 11 street names.

12 **3.1. Verification systems**

13 Verification systems separate two classes: genuine and impostor verification
 14 attempts. By considering the combination task as a pattern classification problem in
 15 the M -dimensional space, Bayesian minimization of the misclassification cost results
 16 in the likelihood ratio combination function²⁵:

$$17 \quad f_{lr}(s^1, \dots, s^M) = \frac{p_{\text{gen}}(s^1, \dots, s^M)}{p_{\text{imp}}(s^1, \dots, s^M)} \quad (2)$$

18 p_{gen} and p_{imp} are M -dimensional densities of score tuples $\{s^1, \dots, s^M\}$ corresponding
 19 to the two classes — genuine and impostor verification attempts. We can estimate
 20 the densities p_{gen} and p_{imp} from the training data and use the above formula to
 21 calculate the combined score and threshold it. Alternatively, generic classification
 22 methods such as neural networks or SVMs can be used for direct classification of
 23 genuine and impostor classes.

24 **3.2. Identification systems**

25 We wish to investigate whether the likelihood ratio function found to be optimal for
 26 verification systems will be also optimal for identification systems. Suppose we
 27 performed a match of the input sample by all M matchers against all N classes and
 28 obtained MN matching scores $\{s_i^j\}_{i=1, \dots, N; j=1, \dots, M}$. Assuming equal prior class prob-
 29 abilities, the Bayes decision theory states that in order to minimize the misclassifi-
 30 cation rate, the sample should be classified as the one with the highest value of the
 31 likelihood function $p(\{s_i^j\}_{i=1, \dots, N; j=1, \dots, M} | \omega_i)$. Thus, for any two classes ω_1 and ω_2 we
 32 can classify the input as ω_1 rather than ω_2 if

$$33 \quad p(\{s_i^j\}_{i=1, \dots, N; j=1, \dots, M} | \omega_1) > p(\{s_i^j\}_{i=1, \dots, N; j=1, \dots, M} | \omega_2) \quad (3)$$

34 Let us make an assumption that the scores assigned to each class are sampled
 35 independently from scores assigned to other classes; scores assigned to genuine class

are sampled from the M -dimensional genuine score density, and scores assigned to impostor classes are sampled from the M -dimensional impostor score density:

$$\begin{aligned} & p(\{s_i^j\}_{i=1,\dots,N;j=1,\dots,M}|\omega_i) \\ &= p(\{s_1^1, \dots, s_1^M\}, \dots, \{s_{\omega_i}^1, \dots, s_{\omega_i}^M\}, \dots, \{s_N^1, \dots, s_N^M\}|\omega_i) \\ &= p_{\text{imp}}(s_1^1, \dots, s_1^M) \dots p_{\text{gen}}(s_{\omega_i}^1, \dots, s_{\omega_i}^M) \dots p_{\text{imp}}(s_N^1, \dots, s_N^M) \end{aligned} \quad (4)$$

After substituting (4) in (3) and canceling out the common factors we obtain the following inequality for accepting class ω_1 (rather than ω_2):

$$p_{\text{gen}}(s_{\omega_1}^1, \dots, s_{\omega_1}^M) p_{\text{imp}}(s_{\omega_2}^1, \dots, s_{\omega_2}^M) > p_{\text{imp}}(s_{\omega_1}^1, \dots, s_{\omega_1}^M) p_{\text{gen}}(s_{\omega_2}^1, \dots, s_{\omega_2}^M) \quad (5)$$

or

$$\frac{p_{\text{gen}}(s_{\omega_1}^1, \dots, s_{\omega_1}^M)}{p_{\text{imp}}(s_{\omega_1}^1, \dots, s_{\omega_1}^M)} > \frac{p_{\text{gen}}(s_{\omega_2}^1, \dots, s_{\omega_2}^M)}{p_{\text{imp}}(s_{\omega_2}^1, \dots, s_{\omega_2}^M)} \quad (6)$$

The terms in each part of the above inequality are exactly the values of the likelihood ratio function f_{lr} calculated for classes ω_1 and ω_2 . Thus, the class maximizing the MN -dimensional likelihood function of inequality (3) is the same as the class maximizing the M -dimensional likelihood ratio function of inequality (6). Thus the likelihood ratio combination rule is optimal under the assumption of score independence. Our goal is to show that this assumption does not generally hold for real-life matchers, and, as a result, likelihood ratio combination method might be detrimental for the performance of the matching system.

It must be noted, *that the score independence assumption refers to scores assigned to different classes by the same matcher* ($\{s_i^j\}_{i=1,\dots,N}$: rows in Fig. 1), *but not to the scores assigned to the same class by different matchers*. The latter score dependence has been investigated a number of times in classifier combination research with respect to the concept of classifier diversity (e.g. Ref. 7). We are interested in the former dependence,²³ which has received little attention thus far in the research community.^{8,19}

The dependence of the matching scores obtained during a single identification trial is usually not taken into account by practitioners.^{5,12,18} Apparently, all matching scores are derived independently from each other: the same matching process is applied repeatedly to all enrolled biometric templates or all lexicon words, and the matching score for one class is not influenced by the presence of other classes or the matching scores assigned to other classes. So it might seem that the matching scores are independent, but this is rarely true in practice. The main reason for the assumption to not hold is that all the matching scores produced during an identification trial are derived using the same input signal. For example, a fingerprint matcher, whose matching scores are derived from the number of matched minutia in enrolled and input fingerprint, will produce low scores for all enrolled fingerprints if the input fingerprint has only a few minutiae. Similarly, if the quality of the sensor is poor, all enrollees may receive a low score.

1 In our experiments, we measured the correlations between genuine scores and
 3 impostor scores produced in the same identification trials (Sec. 5.3), and obtained
 5 significant correlation values, especially for the considered word recognizers. The
 7 existence of such dependence between genuine and impostor scores increases the
 chances of the diminished performance of the likelihood ratio combination rule and
 its nonoptimality.

9 **4. Illustrative Examples**

11 In order to further prove our claim, we present two examples that show that optimal
 13 combination functions for verification and identification systems are not necessarily
 the same. The examples also show that the derivation of the optimal combination
 function for identification systems is actually a nontrivial task.

15 **4.1. Example 1**

17 Let X_{gen} , X_{imp} and Y be independent two-dimensional random variables, and sup-
 19 pose that genuine scores in our identification system are sampled as a sum of X_{gen}
 and Y : $\mathbf{s}_{\text{gen}} = \mathbf{x}_{\text{gen}} + \mathbf{y}$, and impostor scores are sampled as a sum of X_{imp} and Y :
 21 $\mathbf{s}_{\text{imp}} = \mathbf{x}_{\text{imp}} + \mathbf{y}$, $\mathbf{x}_{\text{gen}} \sim X_{\text{gen}}$, $\mathbf{x}_{\text{imp}} \sim X_{\text{imp}}$ and $\mathbf{y} \sim Y$. Bold symbols here denote two-
 dimensional vector in the space (s^1, s^2) . The variable Y provides the dependence
 between scores in identification trials. We assume that its value \mathbf{y} is the same for all
 23 scores in any one identification trial.

25 Let X_{gen} and X_{imp} have gaussian densities $p_{X_{\text{gen}}}(s^1, s^2)$ and $p_{X_{\text{imp}}}(s^1, s^2)$ with unit
 covariance matrices. For any value of \mathbf{y} , conditional densities of genuine and
 27 impostor scores $p_{X_{\text{gen}}+Y|Y=\mathbf{y}}(s^1, s^2)$ and $p_{X_{\text{imp}}+Y|Y=\mathbf{y}}(s^1, s^2)$ are also gaussian and
 independent. Since these gaussians have the same covariance matrices, the optimal
 29 decision surfaces separating these two classes coincide with the contours of
 $s^1 + s^2 = c$.²¹ The optimal combination rule for such conditional distributions co-
 31 incides with the likelihood ratio combination function $f(s^1, s^2) = s^1 + s^2$, and this
 rule will be optimal for every identification trial and its associated value \mathbf{y} . The rule
 itself does not depend on the value of \mathbf{y} , so we can use it for every identification trial,
 33 and this is our optimal combination rule for the identification system. Figure 2(b)
 shows the contours of the optimal combination function in this identification system.

35 On the other hand, this rule might not be optimal for the verification system
 defined by the above score distributions. For example, if Y is uniformly distributed
 37 on the interval $0 \times [-1, 1]$, then the distributions of genuine and impostor scores
 $X_{\text{gen}} + Y$ and $X_{\text{imp}} + Y$ will be as shown in Fig. 2(a) and the optimal combination
 39 rule separating them will be as shown in Fig. 2(c). By changing the distribution of Y
 and thus the character of dependence between genuine and impostor scores, we will
 41 also be changing the optimal combination rule for the verification system. At the
 same time, the optimal combination rule for identification system will stay the
 same — $f(s^1, s^2) = s^1 + s^2$.

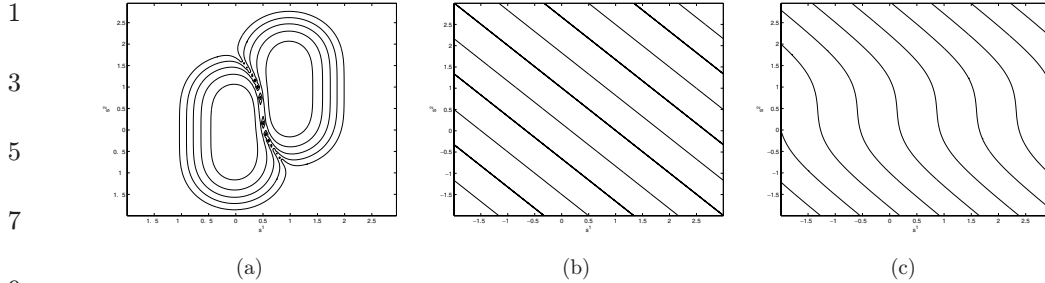


Fig. 2. (a) Two-dimensional distributions of genuine and impostor scores, for example, (b) Contours of optimal combination rule in identification system, (c) Contours of the likelihood ratio combination function.

If all that we know is the overall score distributions [Fig. 2(a)], then we do not have enough information to find the optimal combination function for the identification system case. If the scores are generated by the initial construction, linear combination function in Fig. 2(b) is the optimal combination function. If the score vectors having distributions in Fig. 2(a) are independent on their own, then the likelihood ratio combination in Fig. 2(c) is optimal for the identification system. Thus, there could be different optimal combination functions for identification systems with scores distributed as in Fig. 2(a), and the difference is determined by the nature of the score dependencies in identification trials.

Figures 2(b) and 2(c) show the possible optimal combination functions for identification and verification systems. This example illustrates that when searching for the optimal combination function one must take into account the mode (verification or identification) of the system.

4.2. Example 2

In this example, we are combining the scores of two matchers in an identification system with the number of classes, N , equal to 2. Thus matcher j , $j = 0$ or 1, outputs two scores s_1^j and s_2^j , with one of these scores being genuine, s_{gen}^j , and the other score being impostor, s_{imp}^j . Suppose, that the scores of matchers are sampled from bivariate normal distribution: $\{s_{\text{gen}}^j, s_{\text{imp}}^j\} \sim N(\{1, 0\}, \Sigma_j)$, with

$$\Sigma_1 = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \quad \text{and} \quad \Sigma_2 = \begin{pmatrix} 1 & \lambda \\ \lambda & 1 \end{pmatrix}$$

Thus the two scores of matcher 1 are independent and the two scores of matcher 2 are dependent if $\lambda \neq 0$. The marginal distributions of genuine scores of both matchers are normal $N(1,1)$, and the marginal distributions of impostor scores of both matchers are normal $N(0,1)$. Further, we will assume that the scores related to two matchers are independent; so the joint distribution of two genuine scores is normal $\{s_{\text{gen}}^1, s_{\text{gen}}^2\} \sim N(\{1, 1\}, I)$ and the joint distribution of two impostor scores is normal $\{s_{\text{imp}}^1, s_{\text{imp}}^2\} \sim N(\{0, 0\}, I)$, I is unit matrix.

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1 If this system operates in verification mode, then the optimal score combination
 3 function, likelihood ratio, has same contours as $s^1 + s^2 = c$, and therefore, we can
 take $f_{lr}(s^1, s^2) = s^1 + s^2$ as our optimal combination function for the verification
 5 system. The distributions of genuine, $\{s_{\text{gen}}^1, s_{\text{gen}}^2\}$, and impostor, $\{s_{\text{imp}}^1, s_{\text{imp}}^2\}$, score
 pairs do not depend on λ , and optimal combination function for verification system,
 7 $f_{lr}(s^1, s^2)$, is the same for any choice of λ . But, as we show next, for the identification
 system the situation is different: optimal combination function and the performance
 of the combined system will depend on λ .

9 First, we can measure the identification system performance of the single second
 matcher for different values of λ . Table 1 presents some performance numbers de-
 11 rived by numerically integrating joint density of scores $p(s_{\text{gen}}^2, s_{\text{imp}}^2) = N(\{1, 0\}, \Sigma_2)$
 over the area $s_{\text{gen}}^2 > s_{\text{imp}}^2$. The identification system performance increases with the
 13 increase of λ . Intuitively this can be explained as following: if we have a positive
 correlation between genuine and impostor scores, for a high impostor score we have
 15 bigger probability that genuine will also be high, and the identification attempt will
 still succeed; similarly for low genuine scores we have bigger probability of even lower
 17 impostor scores. For negatively correlated scores ($\lambda < 0$) we observe a decrease in
 performance.

19 In order to calculate the identification system performance of combination
 function f , we numerically integrate $p(s_{\text{gen}}^1, s_{\text{gen}}^2, s_{\text{imp}}^1, s_{\text{imp}}^2) = p(s_{\text{gen}}^1, s_{\text{imp}}^1)p(s_{\text{gen}}^2, s_{\text{imp}}^2)$
 21 over the region $f(s_{\text{gen}}^1, s_{\text{gen}}^2) > f(s_{\text{imp}}^1, s_{\text{imp}}^2)$. The performance of the likelihood ratio
 combination function $f = f_{lr}$ is given in the fourth row in Table 1. Its performance
 23 reflects the change in performance of matcher 2: the better matcher 2 performs, the
 better is the performance of likelihood ratio combination. But notice that for large
 25 values of λ (e.g. $\lambda = 0.7$) the performance of likelihood ratio gets worse than the
 performance of the single matcher 2. The decrease in performance clearly indicates
 27 that likelihood ratio might not be an optimal combination function for identification
 systems. It is also possible to perform simple experiments by considering weighted
 29 sum combination functions $f_w(s^1, s^2) = ws^1 + (1 - w)s^2$, with bigger weight assigned
 to matcher 2 (with better performance in identification mode); by the proper choice
 31 of w it is easy to achieve better performance than using f_{lr} .

33 It turns out that it is possible to exactly derive the optimal combination function
 for the identification system in our example. Suppose that in one identification trial,
 we obtained the following scores from both matchers: $\{s_1^1, s_2^1\}$ from matcher 1 and
 35

37 Table 1. Identification system performance (the frequency of top score being
 genuine) of single matchers and their combinations for Example 2.

	λ	0	0.3	0.5	0.7	-0.5
39	Matcher 1	76.01%	76.01%	76.01%	76.01%	76.01%
	Matcher 2	76.01%	80.08%	84.11%	90.13%	71.81%
41	Likelihood Ratio	84.13%	86.09%	87.58%	89.25%	81.44%
	Optimal Combination	$s_1 + s_2$	$s_1 + \frac{10}{7}s_2$	$s_1 + 2s_2$	$s_1 + \frac{10}{3}s_2$	$s_1 + \frac{2}{3}s_2$
	Optimal Performance	84.13%	86.47%	88.96%	92.95%	81.93%

1 $\{s_1^2, s_2^2\}$ from matcher 2. The combination function f produces combined scores $S_1 =$
 3 $f(s_1^1, s_1^2)$ and $S_2 = f(s_2^1, s_2^2)$. By comparing S_1 and S_2 , we decide which of two classes,
 5 1 or 2, is genuine or impostor. In order to minimize the classification error, we have to
 use optimal Bayesian classification: classify the sample as class 1 instead of class 2, if

$$7 \quad p(\{s_1^1, s_2^1\}, \{s_1^2, s_2^2\} | \text{class 1 is genuine})$$

$$9 \quad > p(\{s_1^1, s_2^1\}, \{s_1^2, s_2^2\} | \text{class 2 is genuine}). \quad (7)$$

10 So, the optimal combination function f should be such that $f(s_1^1, s_1^2) > f(s_2^1, s_2^2)$ if
 11 and only if Eq. (7) holds. After utilizing the independence of matchers ($p(\{s_1^1, s_2^1\},$
 13 $\{s_1^2, s_2^2\} | \dots) = p(\{s_1^1, s_2^1\} | \dots) p(\{s_1^2, s_2^2\} | \dots)$), we substitute the given normal
 densities of score pairs produced by each matcher:

$$15 \quad p(\{s_1^j, s_2^j\} | \text{class 1 is genuine}) = N\left(\begin{pmatrix} s_1^j \\ s_2^j \end{pmatrix}; \begin{pmatrix} 1 \\ 0 \end{pmatrix}, \Sigma_j\right) \quad (8)$$

$$17 \quad p(\{s_1^j, s_2^j\} | \text{class 2 is genuine}) = N\left(\begin{pmatrix} s_2^j \\ s_1^j \end{pmatrix}; \begin{pmatrix} 1 \\ 0 \end{pmatrix}, \Sigma_j\right) \quad (9)$$

19 After substitution, we can transform Eq. (7) into the following inequality:

$$21 \quad s_1^1 + s_1^2 * \frac{1}{1-\lambda} > s_2^1 + s_2^2 * \frac{1}{1-\lambda} \quad (10)$$

23 Therefore, we can take the following function as the optimal combination function
 25 for the identification system in our example:

$$27 \quad f_{\text{id}}(s^1, s^2) = s^1 + s^2 * \frac{1}{1-\lambda} \quad (11)$$

29 The combination based on f_{id} coincides with the combination based on f_{r} only when
 $\lambda = 0$. In other cases, f_{id} performs better than f_{r} in the identification operating
 31 mode. The last two rows in Table 1 contain samples of optimal combination function
 f_{id} for the identification mode and the corresponding correct identification rates. In
 33 all cases, f_{id} performs better than any single matching participating in combination.

35 4.3. Discussion

37 The examples presented in this section underline the complexity of the task of finding
 an optimal combination function for identification systems. Given sufficient number
 of training genuine and impostor score samples, we might be able to approximate the
 39 genuine and impostor score densities (e.g. Fig. 2(a)). Given such density approxi-
 mations, we can deduce the optimal combination function for verification systems
 41 (Fig. 2(c)). But we would still not have a good method to derive the optimal com-
 bination function for identification systems (Fig. 2(b)). It is possible that the like-
 hood ratio combination rule of Fig. 2(c) is the optimal combination function in

1 identification system. It will certainly be the case if the identification trial scores are
independent.

3 Suppose that score dependence had to be accounted for between different classes
and an optimal combination function had to be derived for identification systems as
5 in the second example. The first problem that we would have faced is to properly
represent the joint density of a set of scores produced by a single matcher, e.g.
7 $p(s_1^1, s_2^1, \dots, s_N^1)$. If the number of classes, N , is large, we might want to reduce the
number of variables by considering score set statistics. The second problem would be
9 the construction of the combination function f_{id} given the reconstructed joint densities.
Note, that in order to derive a combination function from Eq. (7), scores are to
11 be separated related to different classes, so that the combination function would
operate only on the scores related to a single class: $f(s_1^1, s_1^2) > f(s_2^1, s_2^2)$. We were
13 successful in doing so in Example 2 only due to a particular form of score densities
(gaussian). In the general case, such derivation might be difficult to achieve.

15 As an additional consequence of our examples, we can assert that any score
normalization based on reconstructed genuine and impostor score densities does not
17 provide an answer to finding optimal combination function in identification systems.
The only normalizations which might be beneficial for combinations in identification
19 systems (assuming that we have a trainable combination algorithm able to take care
of simple score translation normalizations) will be based on considering sets of
21 identification trial scores similar to T-normalization.⁴ Our paper²³ contains a deeper
discussion on such normalizations.

23 A final corollary of the examples is that the training of optimal combination
function for identification systems requires simultaneous consideration of the genuine
25 and impostor scores from the same identification trials. In particular, we cannot
simply take a set of all impostor scores and mix them. By doing so, the training will
27 take place on the genuine and impostor densities, giving a combination algorithm
trained for verification rather than for identification systems.

31 5. Experiments

In this section, we present the experimental results to support the claims made in this
33 paper. First, in Secs. 5.1 and 5.2, we introduce the considered identification systems,
handwritten word recognition and biometric person identification, and define the
35 testing procedures. The next section presents the analysis of the dependence between
scores assigned to different classes in all considered matchers. Section 5.5 presents the
37 results on likelihood ratio and the weighted sum combination methods.

39 5.1. *Handwritten word recognizers*

41 We consider the application of handwritten word recognizers in the automatic
processing of United Kingdom mail. The destination information of the mail piece
contains the name of the postal town or county. After automatic segmentation of the

1 mail piece image, the goal of the handwritten word recognizer is to match the hy-
2 hypothesized town or county word image against a lexicon of possible names, which
3 contains 1681 entries.

4 We use two handwritten word recognizers for this application: Character Model
5 Recognizer (CMR)¹⁰ and Word Model Recognizer (WMR).¹⁶ Both recognizers
6 employ similar approaches to word recognition: they oversegment the word images,
7 match the combinations of segments to characters and derive a final matching score
8 for each lexicon word as a function of the character matching scores.

9 Our data consists of three sets of word images of approximately the same quality.
10 The data was initially provided as these three subsets and therefore, we did not
11 regroup them. The images were manually truthed and only those images containing
12 any of the 1681 lexicon words were retained. The word recognizers were run on these
13 images and their match scores for all 1681 lexicon words were saved. Note, that both
14 recognizers reject some lexicon entries if, for example, the lexicon word is too short or
15 too long for the presented image. We assume that in real systems, such rejects will be
16 dealt with separately (it is possible that the lexicon word corresponding to image
17 truth will be rejected), but for our combination experiments we keep only the scores
18 of those lexicon words which are not rejected by either of the recognizers. Thus for
19 each image I_k we have a variable number N_k of score pairs $(s_i^{\text{cmr}}, s_i^{\text{wmr}})$, $i = 1, \dots, N_k$
20 corresponding to nonrejected lexicon words. One of these pairs corresponds to the
21 true word of the image which we refer to as “genuine” scores, and the other
22 “impostor” score pairs correspond to nontruth words.

23 After discarding images with nonlexicon words, and images where the truth word
24 was rejected by either recognizer, we are left with three sets of 2654, 1723 and 1770
25 images and related sets of score pairs. We will refer to the attempt of recognizing a
26 word image as an identification trial. Thus each identification trial has a set of score
27 pairs $(s_i^{\text{cmr}}, s_i^{\text{wmr}})$, $i = 1, \dots, N_k$ with one genuine score pair and $N_k - 1$ impostor
28 pairs. The scores of each recognizer were also linearly normalized so that each score is
29 in the interval $[0,1]$ and the bigger score implies a better match.

30 Since our data was already separated into three subsets, we used this structure for
31 producing the training and testing sets. Each experiment was repeated three times.
32 Each time one subset was used as a training set, and the other two sets were used as test
33 sets. The final results are derived as averages of these three training/testing phases.

35 5.2. Biometric person matchers

36 We used biometric matching score set BSSR1 distributed by NIST.¹ This set con-
37 tains matching scores for a fingerprint matcher and two face matchers “C” and “G”.
38 Fingerprint matching scores are given for left index “li” finger matches and right
39 index “ri” finger matches. For experiments, we used four combinations involving
40 both fingerprint and face score subsets: “li&C”, “li&G”, “ri&C” and “ri&G”

41 Though the BSSR1 score set has a subset of scores obtained from the same
physical individuals, this subset is rather small — 517 identification trials with 517

1 enrolled persons. In our previous experiments²² we used this subset, but the number
 2 of failed identification attempts for most experiments was less than 10 and it is
 3 difficult to compare algorithms with those few negatives. Therefore, we used larger
 4 subsets of fingerprint and face matching scores of BSSR1 by creating virtual persons.
 5 The fingerprint scores of a virtual person come from a physical person and the face
 6 scores come from a different individual. The scores are not reused, and thus we are
 7 limited to a maximum of 6000 identification trials and a maximum of 3000 classes (or
 8 enrolled persons). Some enrollees and some identification trials are also required to be
 9 discarded since the corresponding matching scores were invalid probably due to
 10 enrollment errors. Finally, we split the data into two parts — 2991 identification
 11 trials with 2997 enrolled persons, with each part used as training and testing sets in
 12 two phases.

13 **5.3. Dependence of matching scores assigned to different classes**

14 We have made a key observation in Sec. 3 that the likelihood ratio combination rule
 15 might be optimal for identification systems if the matching scores assigned to the
 16 different classes by the same classifier are statistically independent. In order to test
 17 the score independence assumption we calculated the correlations between the
 18 matching scores assigned to the different classes: between genuine and impostor
 19 scores, and between two impostor scores obtained in the same identification trial.
 20 The results are presented in Fig. 2 for all matchers on our datasets.

21 The calculation of correlation values was performed using a subset of 2654
 22 identification trials for word recognizers and one subset of 2991 identification trials
 23 for biometric matchers. In each trial, 50 random impostor scores were selected for
 24 calculating correlations. As a result, the calculation of $\text{cor}(s_{\text{gen}}, s_{\text{imp},i})$ involves
 25 averaging of 2654×50 terms and the calculation of $\text{cor}(s_{\text{imp},i}, s_{\text{imp},j})$ involves aver-
 26 aging of $2654 \times (50 \times 49/2)$ terms for word recognizers, and correspondingly $2991 \times$
 27 50 and $2991 \times (50 \times 49/2)$ terms for biometric matchers. Nonzero correlation values
 28 confirm our hypothesis that the score independence assumption does not hold.

29 In addition, Ref. 25 contains calculations of correlation values between genuine
 30 scores and some functions of the impostor scores in the identification trials, for
 31 example, the correlation between the genuine score and the maximum of impostor
 32 scores obtained in the same trial. Those correlations were greater than what is

33 Table 2. Correlations between scores assigned to
 34 different classes during same identification trials.

35 Matchers	$\text{cor}(s_{\text{gen}}, s_{\text{imp},i})$	$\text{cor}(s_{\text{imp},i}, s_{\text{imp},j})$
36 CMR	0.043941	0.102119
37 WMR	0.364168	0.409941
38 li	0.106033	0.125387
39 ri	0.138155	0.149010
40 C	0.039175	0.094667
41 G	0.067829	0.125417

1 currently presented in Fig. 2. This indicates that the dependence between scores
2 might be complex. Modeling these dependences constitutes a part of our work on
3 classifier combinations utilizing identification models.²³

5 5.4. Description of combination algorithms

7 We have explored two combination methods in this paper: likelihood ratio and the
8 weighted sum. For the likelihood ratio combination, we reconstructed the densities
9 using the Parzen window method with Gaussian kernels. The window widths are
10 found by maximum likelihood leave-one-out cross validation method on a training
11 set. Note that the reconstructed densities $p_{\text{gen}}(s^1, s^2)$ and $p_{\text{imp}}(s^1, s^2)$ of the like-
12 likelihood ratio combination function 2 are two-dimensional. Given a large number of
13 training samples, using two-dimensional kernels in the Parzen method results in a
14 good approximation of the densities.²⁴

15 We have compared the performance of the likelihood ratio rule with the weighted
16 sum combination rule, which is one of the most frequently used rules in classifier
17 combination tasks. The weighted sum rule is expressed by the combination function
18 $f(s^1, \dots, s^M) = w_1 s^1 + \dots + w_M s^M$. The weights w_j are usually ²⁰ chosen heur-
19 istically so that the better performing matchers have a bigger weight. The optimal
20 weights can also be estimated for linear combinations of classifiers subject to the
21 minimization of classification error.²⁷

22 In our experiments, we have trained the weights so that the number of successful
23 identification trials on the training set is maximized. The previously proposed
24 methods of training resulting in the minimization of classification error ²⁷ are not
25 directly applicable due to much bigger number of classes in our case. Since we have
26 only two matchers in all our configurations, it was possible to utilize a brute-force
27 approach: we calculate the correct identification rate of the combination function
28 $f(s^1, s^2) = w s^1 + (1 - w) s^2$ for different values of $w \in [0, 1]$, and find w corre-
29 sponding to the highest recognition rate. Despite being brute-force, due to simplicity
30 of weighted sum method, this approach was faster to train than likelihood ratio.

31 Note, that for the weighted sum method, as well as for likelihood ratio, we have
32 separate training and testing subsets; the performance of this rule on test sets is
33 slightly lower than the performance on training sets.

35 5.5. Combination results

37 The results of the combination using the likelihood ratio and the weighted sum are
38 shown in Table 3. The numbers in the table refer to the correct identification rates,
39 that is, the percentage of trials in which the genuine score receives the best score
40 compared to all impostor scores of the same identification trial. For comparison, we
41 also present the performance of single matchers used in combination.

Although for biometric combinations, the likelihood ratio combination method
provided similar or better performance than the weighted sum rule, it performed very

Table 3. Correct identification rates for single matchers and their combinations by likelihood ratio and weighted sum.

Matchers	1st Matcher is Correct	2nd Matcher is Correct	Likelihood Ratio	Weighted Sum
CMR&WMR	54.76%	77.18%	69.84%	81.58%
li&C	81.41%	81.18%	97.24%	97.23%
li&G	81.41%	77.48%	95.90%	95.47%
ri&C	88.53%	81.18%	98.23%	98.09%
ri&G	88.53%	77.48%	97.14%	96.82%

poorly in the combination of handwritten word recognizers. In fact, it resulted in a performance lower than the performance of a single word recognizer. This would clearly imply that the likelihood ratio combination method might not be an optimal combination method for identification systems.

In order to verify that likelihood ratio combination for word recognizers was implemented correctly, we measured its performance in verification operating mode. Figure 3 presents ROC curves for likelihood ratio, as well as for weighted sum combination. As we expected, the likelihood ratio outperforms weighted sum and has superior performance with respect to single matchers.

Example 2 in Sec. 4.2 explains why the combination based on likelihood ratio function performs worse than a single matcher WMR. As in example, WMR

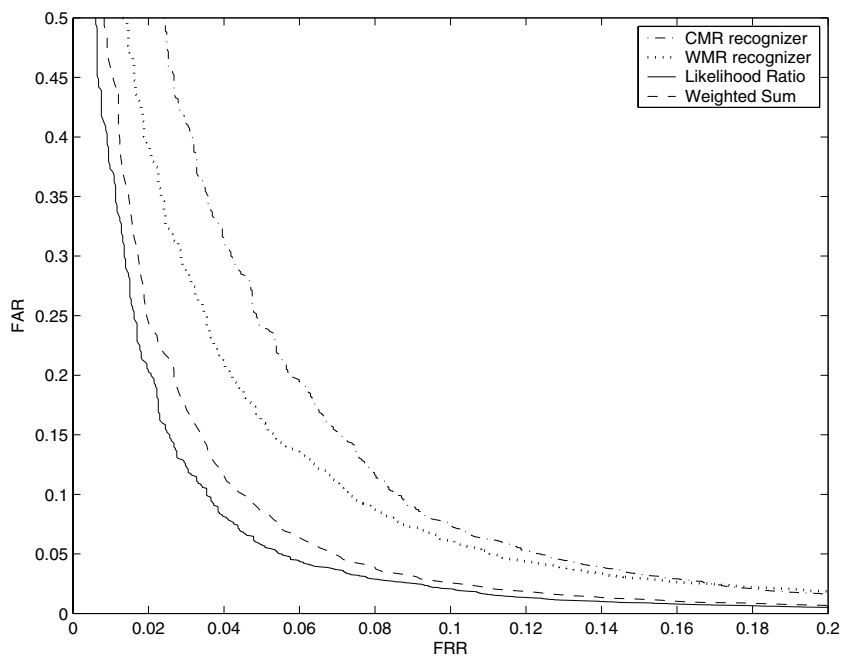


Fig. 3. The verification system performance of word recognizers and their combinations by likelihood ratio and weighted sum.

1 produces strongly dependent matching scores and has better identification system
2 performance, than another combined matcher, CMR. The likelihood ratio fails to
3 take the score dependence of WMR into account.

4 Though the likelihood ratio method seems to perform well for identification sys-
5 tem with biometric matchers, this might not be the optimal combination method. In
6 our previous work²⁶ we have presented some combination methods for identification
7 systems (involving considered NIST BSSR1 datasets) which are able to outperform
8 both likelihood ratio and weighted sum. But we still do not know if the proposed
9 methods are optimal for identification system combinations.

11 6. Summary

12 In this paper, we show that for different operating scenarios of multiclassifier sys-
13 tems, namely verification and identification, we need to construct different combi-
14 nation algorithms to achieve optimal performance. This is due to the frequent
15 dependence among the scores produced by each matcher during a single identifi-
16 cation trial. The optimal combination algorithm for verification systems corresponds
17 to the likelihood ratio combination function. It can be implemented by the direct
18 reconstruction of this function with genuine and impostor score density approxi-
19 mations. Alternatively, many generic pattern classification algorithms can be used to
20 separate the genuine and impostor scores in the M -dimensional score space, where M
21 is the number of combined matchers.

22 The optimal combination algorithm for the identification systems is more difficult
23 to realize. With the help of artificial examples we have shown that it is difficult to
24 express the optimal combination function analytically. The experiments with
25 existing score sets confirm the nonoptimality of likelihood ratio combination method
26 for identification system. Though the weighted sum combination method can be
27 trained for best identification system performance, due to the limited representation
28 ability, it also might not achieve the optimal performance.

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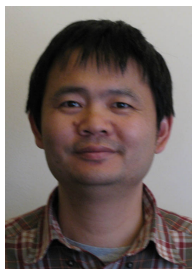
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