

**Applied Cryptography and Computer
Security
CSE 664 Spring 2020**

Lecture 10: Applications of Hash Functions

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Overview

- Going back to our security goal of data integrity:
 - theoretical MAC constructions
 - CBC-MAC
 - HMAC
- Sample applications of hash functions

MAC Algorithms

- Constructing a MAC algorithm from a hash function
 - one approach is to include the key k as part of the hash function input:
$$\text{Mac}_k(x) = h(k||x)$$
 - if the hash function is one-way, we won't be able to recover the key
 - but how about MAC forgery?

MAC Algorithms

- $\text{Mac}_k(x) = h(k||x)$
 - assume we have a message $m = m_1m_2\dots m_t$
 - consider an iterated hash function: $h_0 = IV, h_i = f(m_i, h_{i-1});$
 $h(x) = h_t$
 - then we can extend m by an arbitrary single block b and compute the MAC on $m' = m_1m_2\dots m_tb$
 - compute $\text{Mac}_k(m') = h(k||m||b)$ as $f(\text{Mac}_k(m), b)$
- What if we construct a MAC from a hash function using the key k as the IV for the compression function?

MAC Algorithms

- Hash-Based MAC – HMAC
- Goals:
 - use available hash functions without modifications
 - preserve the original performance of the hash function
 - use and handle keys in a simple way
 - allow replacement of the underlying hash function
 - have a well-understood cryptographic analysis of its strength

MAC Algorithms

- HMAC

- $\text{HMAC}_k(x) = h((K \oplus \text{opad}) || h((K \oplus \text{ipad}) || x))$
- K is the key k padded to a full block
- $\text{ipad} = 0 \times 3636 \dots 36$ and $\text{opad} = 0 \times 5C5C \dots 5C$ are fixed padding constants

- Properties of HMAC:

- efficient
- security is related to that of the underlying hash function
 - we want $k_1 = h(K \oplus \text{opad})$ and $k_2 = h(K \oplus \text{ipad})$ to be rather independent and close to random
 - then HMAC is existentially unforgeable under an adaptive chosen-message attack for messages of any length

MAC Algorithms

- HMAC Security
 - provides greater security than the security of the underlying hash function
 - no known practical attacks if a secure hash function is used and according to the specifications
- In general, HMAC can be attacked by:
 - brute force search on the key space
 - attacks on the hash function

Other Uses of Hash Functions

- Hash Chains

- a method for authenticating multiple user logins or packet streams
- consists of successive application of a hash function to a string
- n applications of the hash function on x is denoted by $h^n(x)$
- this produces a hash chain of length n

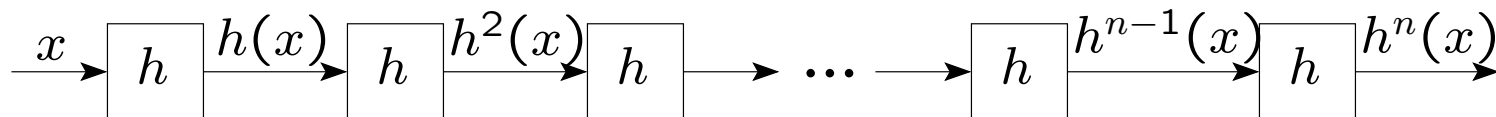
- Example:

- $h^4(x) = h(h(h(h(x))))$ produces a hash chain of length 4

Uses of Hash Functions

- Authentication using hash chains

- user generates a hash chain of length n
- at time 1, the user sends $auth_1 = h^n(x)$ (and possibly authenticates it through other means)
- the recipient stores $auth = auth_1$
- at time 2, the user sends $auth_2 = h^{n-1}(x)$
- the recipient checks whether $h(auth_2) = auth_1$ and, if so, accepts
- the recipient updated $auth = auth_2$
- etc.



Uses of Hash Functions

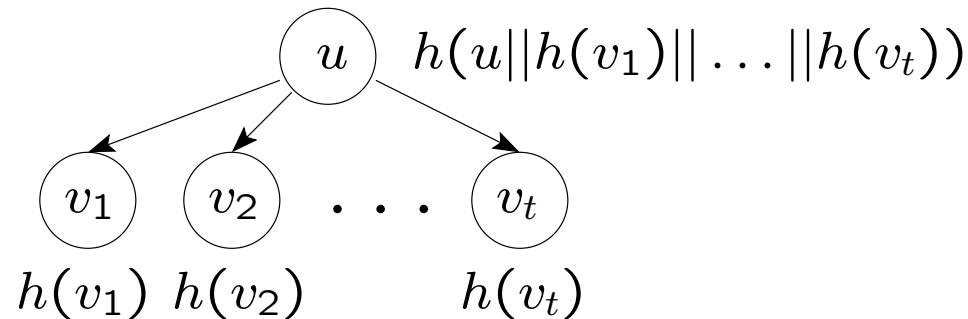
- Why is such authentication secure?
- Authentication in packet streams
 - we can similarly authenticate each packet as belonging to the stream
 - need to take into account packet delivery delay
 - a packet authentication value is opened several packets later
 - see Perrig et al. “Efficient Authentication and Signing of Multicast Streams over Lossy Channels” (2000) for more information

Uses of Hash Functions

- **Merkle Hash Tree**
 - integrity verification mechanism for hierarchically structured documents or databases
 - the technique works on trees only
 - the hash of the tree is computed in the bottom-up fashion
- **Generation of a Merkle hash tree**
 - for a leaf node v , simply compute its hash $h(v)$
 - for a non-leaf node u with children v_1, \dots, v_t , compute its hash as $h(u || h(v_1) || \dots || h(v_t))$

Uses of Hash Functions

- Merkle Hash Tree



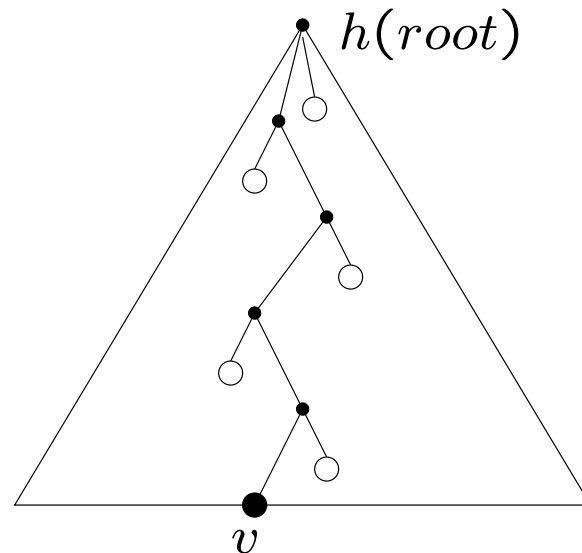
- this computation continues until the hash of the root is computed
- the hash of the root corresponds to the hash of the entire tree

- Integrity verification

- node integrity verification is much faster than hashing the entire tree
- to check node v , obtain hashes of the nodes on the path from v to the root

Uses of Hash Functions

- Integrity verification in Merkle Hash Tree



- your node
- hash is given
- compute the hash

- compute the hash of v and combine it with other hashes on the path to the root
- compare your hash of the root with what you are given
- the node you are authenticating doesn't have to be a leaf

Uses of Hash Functions

- Merkle Hash Tree
 - why does this work?
 - what are the computation savings compared to just applying the hash function to the entire tree?
 - what needs to be done when a node's content changes?

Uses of Hash Functions

- Commitment schemes

- a commitment scheme allows one to “commit” to a message m by computing a committed value com
- it can later be opened to reveal m
- the following properties are required to hold:
 - **hiding property**: commitment com reveals nothing about message m
 - **binding property**: it is infeasible to find another message $m' \neq m$ such that com can be opened to m'

Uses of Hash Functions

- A **commitment scheme** is defined by three algorithms
 - **Gen**: randomized algorithm that takes a security parameter 1^n and outputs public parameters params
 - **Com**: randomized algorithm that takes params and a message $m \in \{0, 1\}^n$ and outputs commitment com
 - we make the randomness that **Com** uses explicit, denote it by r , and use $\text{com} = \text{Com}(\text{param}, m, r)$
 - **Open**: a deterministic algorithm that decommits to m by typically disclosing m and r
 - the verifier that check whether com is in fact equal to $\text{Com}(\text{params}, m, r)$

Uses of Hash Functions

- The security properties of a **commitment scheme** can be formally defined as two experiments
 - to achieve **hiding**, \mathcal{A} chooses m_0, m_1 , receives a commitment to one of them and is asked to determine which message was used
 - to achieve **binding**, \mathcal{A} is challenged to create a commitment com and two different openings for it (m, r) and (m', r')
- We require that a commitment scheme is **secure** if
 - the probability of succeeding in the hiding experiment is at most negligibly larger than $1/2$ and
 - the success in the binding experiment is at most negligible

Uses of Hash Functions

- We can use **hash functions** to create a **commitment scheme** (in the random oracle model):
 - Gen takes a security parameter 1^n and chooses an appropriate hash function h
 - to commit to m , choose uniform $r \in \{0, 1\}^n$ and output $\text{com} := h(m||r)$
 - hiding follows because adversary can query $h(*||r)$ with only a negligible probability
 - binding follows from the collision resistant property of h

Confidentiality + Integrity

- How do we use a MAC in combination with encryption?

- message **authentication**

- $A \xrightarrow{m, \text{Mac}_k(m)} B$

- **encrypt and authenticate**

- $A \xrightarrow{\text{Enc}_{k_1}(m), \text{Mac}_{k_2}(m)} B$

- **authenticate then encrypt**

- $A \xrightarrow{\text{Enc}_{k_1}(m, \text{Mac}_{k_2}(m))} B$

- **encrypt then authenticate**

- $A \xrightarrow{\text{Enc}_{k_1}(m), \text{Mac}_{k_2}(\text{Enc}_{k_1}(m))} B$

Confidentiality + Integrity

- Which construction is good for achieving both objectives?
 - how do we define “good”?
- We want a combination that **always** achieves both confidentiality and integrity
 - given any CPA-secure encryption scheme and any secure MAC scheme, the construction must achieve both goals
 - if there are secure encryption and MAC schemes using which a construction doesn't achieve both goals, we say it is insufficient

Confidentiality + Integrity

- How do we combine two schemes into one?
 - we are given encryption $E = (\text{Gen}_E, \text{Enc}, \text{Dec})$ and MAC $M = (\text{Gen}_M, \text{Mac}, \text{Vrfy})$
 - we build message transmission scheme $T = (\text{Gen}, \text{EncMac}, \text{DecVrfy})$
- **Correctness** is defined as before
- **Security** is based on meeting the requirements of two experiments: authenticated communication and confidentiality experiments
 - there is a single authenticated communication experiment $\text{AuthComm}_{\mathcal{A},T}(n)$

Confidentiality + Integrity

- Analysis of our constructions:
 - encrypt and authenticate
 - transmitting $\text{Mac}_{k_2}(m)$ may leak information about m
 - authenticate then encrypt
 - has a chosen-ciphertext attack against the general version, which has been successfully applied in practice
 - tampering with ciphertext might permit predictable changes to the encrypted content
 - encrypt then authenticate
 - satisfies the definition and is CCA-secure
- The keys k_1 and k_2 must be different!

Authenticated Encryption

- Do I have to use encryption and MAC separately or are there **authenticated encryption modes**?
 - recently, authenticated encryption modes have been proposed
- Some good reads:
 - <https://blog.cryptographyengineering.com/2012/05/19/how-to-choose-authenticated-encryption/>
 - <https://stackoverflow.com/questions/1220751/how-to-choose-an-aes-encryption-mode-cbc-ecb-ctr-ocb-cfb>

Authenticated Encryption

- Good options to consider:
 - **Offset Codebook (OCB) mode**
 - state of the art in authenticated encryption
 - proposed internet standard
 - has licensing restrictions
 - see <http://web.cs.ucdavis.edu/~rogaway/ocb/ocb-faq.htm> for more information
 - **Galois/Counter Mode (GCM)**
 - does not have licensing restrictions
 - can be used as an alternative for commercial software

Summary

- Hash functions have many uses:
 - data integrity
 - data and user authentication
 - in various protocols as a one-way function
- Combining confidentiality and integrity requires care
- Next time:
 - public key cryptography!
 - number theory