MTH 142 College Calculus II Course Guide University at Buffalo

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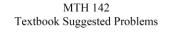
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1 Introduction: How to use the Course Guide

The purpose of this document is to provide to the student the **MTH 142** course learning objectives. Any learning objective listed here may be assessed on the MTH 142 final exam.

This list of learning objectives is broken by section of the textbook (*J. Stewart, Calculus, Early Transcendental MTH 141, 142, 8th custom UB ed.*). The Course Guide should be used together with the MTH 142 Textbook Suggested Problems. Figure 1.1 illustrates how to use the Course Guide and the Textbook Suggested Problems.



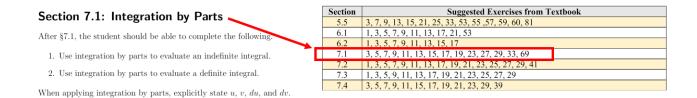


Figure 1.1: Learning objectives for §7.1 are mapped to exercises in the textbook.

Section 5.5: The Substitution Rule

After §5.5, the student should be able to complete the following.

- 1. When appropriate, apply the Substitution Rule to evaluate an indefinite integral.
- 2. When appropriate, apply the Substitution Rule to evaluate a definite integral.

Section 6.1: Areas Between Curves

After §6.1, the student should be able to complete the following.

1. Given a region bounded by curves, use a definite integral to find the area of the region.

Section 6.2: Volumes

After §6.2, the student should be able to complete the following.

- 1. Use the definite integral to find the volume of the solid obtained by rotating a region about a designated line. As part of the solution, the student is expected to complete the following.
 - a) Sketch a typical approximating disk/washer.
 - b) State the inner radius and outer radius of a typical disk/washer.

Section 7.1: Integration by Parts

After §7.1, the student should be able to complete the following.

- 1. Use integration by parts to evaluate an indefinite integral.
- 2. Use integration by parts to evaluate a definite integral.

When applying integration by parts, explicitly state u, v, du, and dv.

Section 7.2: Trigonometric Integrals

After §7.2, the student should be able to complete the following.

- 1. Evaluate an integral of the form: $\int \sin^m x \cos^n x \, dx$.
- 2. Evaluate an integral of the form: $\int \tan^m x \sec^n x \, dx$.

Section 7.3: Trigonometric Substitution

After §7.3, the student should be able to complete the following.

- 1. Use a trigonometric substitution to evaluate an indefinite integral. The answer should involve the same variable as the original given integral (e.g., if the given indefinite integral involves the variable x then the answer should be an explicit function of x).
- 2. Use a trigonometric substitution to evaluate a definite integral.

Section 7.4: Integration of Rational Functions by Partial Fractions

After §7.4, the student should be able to complete the following.

- 1. Using Cases I III of the section, find a partial fraction decomposition of a rational function.
- 2. Evaluate the integral of a rational function using a partial fraction decomposition.

Section 7.5: Strategy for Integration

After §7.5, the student should be able to complete the following.

- 1. Use strategies for integration to evaluate a given indefinite integral. The student determines the method.
- 2. Use strategies for integration to evaluate a given definite integral. The student determines the method.

Section 7.8: Improper Integrals

After §7.8, the student should be able to complete the following.

- 1. Determine whether an improper integral is converge or divergent. If convergent, evaluate the integral.
- 2. Determine for which values of p the improper integral $\int_{1}^{\infty} \frac{1}{x^{p}} dx$ is convergent and for which values of p the integral is divergent.
- 3. Use the Comparison Theorem to determine whether an improper integral is convergent or divergent.

Section 8.1: Arc Length

After §8.1, the student should be able to complete the following.

1. Use an arc length formula to find the exact length of a curve over an interval.

Section 10.1: Curves Defined by Parametric Equations

After §10.1, the student should be able to complete the following.

- 1. Given parametric equations x = f(t), y = g(t) for a curve, sketch the curve using the parametric equations to plot points. Indicate, using an arrow, the direction in which the curve is traced as t increases.
- 2. Given parametric equations x = f(t), y = g(t) for a curve, eliminate the parameter to find a Cartesian equation of the curve.

Section 10.2: Calculus with Parametric Curves

After §10.2, the student should be able to complete the following.

- 1. Given parametric equations x = f(t), y = g(t) for a curve, find dy/dx if $dx/dt \neq 0$.
- 2. Given parametric equations x = f(t), y = g(t) of a curve for $\alpha \le t \le \beta$, find the exact length of the curve.

Section 10.3: Polar Coordinates

After §10.3, the student should be able to complete the following.

- 1. Plot points given polar coordinates (r, θ)
- 2. Convert a point $P(r, \theta)$ in polar coordinates to Cartesian coordinates. Use $x = r \cos \theta$, $y = r \sin \theta$.
- 3. Convert a point (x, y) in Cartesian coordinates to polar coordinates. Use $x^2 + y^2 = r^2$ and $\tan \theta = y/x$.
- 4. Sketch the region in the plane consisting of points whose polar coordinates satisfy inequality conditions.
- 5. Sketch a polar curve $r = f(\theta)$.

Section 11.1: Sequences

After §11.1, the student should be able to complete the following.

- 1. Determine whether a sequence $\{a_n\}$ is convergent or divergent.
- 2. List first terms of a sequence given the general term a_n . For example, list the first 5 terms of the sequence with general term $a_n = \frac{1}{n^2}$.

Section 11.2: Series

After §11.2, the student should be able to complete the following.

- 1. Given an infinite series, find partial sums of the series. For example, given the series $\sum_{n=1}^{\infty} \frac{1}{n^2}$ find the first 4 partial sums s_1 , s_2 , s_3 , and s_4 .
- 2. Given a geometric series:
 - a) Find the common ratio r.
 - b) Use the common ratio r to determine whether the geometric series is convergent or divergent. If the geometric series is convergent, find its sum.
- 3. Use the Test for Divergence to show a series $\sum a_n$ is divergent by showing either $\lim_{n \to \infty} a_n$ DNE or $\lim_{n \to \infty} a_n \neq 0$, if possible.

Section 11.3: The Integral Test and Estimates of Sums

After §11.3, the student should be able to complete the following.

- 1. Use the Integral Test to test the convergence or divergence of an infinite series.
- 2. State for which values of the parameter p the p-series

$$\sum_{n=1}^{\infty} \frac{1}{n^p}$$

is convergent and for which values of p the series is divergent.

Section 11.4: The Comparison Tests

After §11.4, the student should be able to complete the following.

- 1. Use The Comparison Test to test the convergence or divergence of a series $\sum a_n$ with positive terms. Explicitly state the series $\sum b_n$ to which $\sum a_n$ is compared.
- 2. Use The Limit Comparison Test to test the convergence or divergence of a series $\sum a_n$ with positive terms. Explicitly state the series $\sum b_n$ to which $\sum a_n$ is compared.

Section 11.5: Alternating Series

After §11.5, the student should be able to complete the following.

- 1. Determine if a given series $\sum a_n$ is an alternating series.
- 2. Use the Alternating Series Test to show an alternating series is convergent (when the series satisfies to hypotheses of the test).
- 3. For a convergent alternating series $\sum (-1)^n b_n$, use the Alternating Series Estimation Theorem to estimate the error

$$|R_n| = |s - s_n|$$

where $s = \sum (-1)^n b_n$ and s_n is the *n*th partial sum of the series. (So $s_n \approx s$.)

Section 11.6: Absolute Convergence and the Ratio and Root Tests

After §11.6, the student should be able to complete the following.

- 1. Determine if a series $\sum a_n$ is absolutely convergent or conditionally convergent.
- 2. Use the Ratio Test to determine if a series $\sum a_n$ is convergent or divergent.
- 3. Use the Root Test to determine if a series $\sum a_n$ is convergent or divergent.

Section 11.7: Strategy for Testing Series

After §11.7, the student should be able to complete the following.

- 1. Choose an appropriate method (test) to test a series for convergence or divergence. When testing a series for convergence or divergence, the student should expect to complete the following.
 - (a) State which test is being used.
 - (b) Explicitly show that the assumptions of a test are satisfied (if any assumptions). For example, if applying the Integral Test the student should address conditions that the function f(x) must be continuous, positive, and decreasing on $[1, \infty)$.

Section 11.8: Power Series

After §11.8, the student should be able to complete the following.

- 1. Given a power series $\sum_{n=0}^{\infty} c_n (x-a)^n$:
 - a) Find the radius of convergence R using either the Ratio Test or the Root Test.
 - b) Find the interval of convergence using either the Ratio Test or Root Test. If $0 < R < \infty$, the student must test convergence of the power series at each end point of (a R, a + R).

Section 11.9: Representations of Functions as Power Series

In §11.9, the student learns how to manipulate the power series shown below in Equation 7.1 to construct power series for functions related to $f(x) = \frac{1}{1-x}$ through multiplication by a x^k (k a positive integer), composition, differentiation, and/or antidifferentiation.

$$\frac{1}{1-x} = 1 + x + x^2 + x^3 + \dots = \sum_{n=0}^{\infty} x^n \qquad |x| < 1$$
(7.1)

After §11.9, the student should be able to complete the following.

- 1. Find a power series expression for a function f that can be generated from Equation 7.1 through multiplication by x^k and/or composition of functions (e.g., replace x by g(x) in Equation 7.1).
- 2. Use term-by-term differentiation to express a function as a power series.
- 3. Use term-by-term integration to express a function as a power series.
- 4. If the function f can be expressed as a power series obtained from the power series in Equation 7.1, approximate $\int_a^b f(x) dx$ using the power series.

Section 11.10: Taylor and Maclaurin Series

After §11.10, the student should be able to complete the following.

- 1. Find a Taylor series of a function f centered at a. Find the associated radius of convergence. [Do not show that $R_n(x) \to 0$ as $n \to \infty$.]
- 2. Find Maclaurin series for the following functions. Find the associated radius of convergence for each function. [Do not show that $R_n(x) \to 0$ as $n \to \infty$.]

$$f_1(x) = e^x$$
, $f_2(x) = \sin x$, $f_3(x) = \cos x$, $f_4(x) = \tan^{-1} x$

3. Use a Maclaurin series found in Table 1 of §11.10 to find a Maclaurin series for a function.

Section 11.11: Applications of Taylor Polynomials

After §11.11, the student should be able to complete the following.

1. Assuming f is equal to the sum of its Taylor series centered at a, use the *n*th-degree Taylor polynomial, T_n , of f at a to approximate f near a.