

Two-Way ANOVA

Source	Degrees of freedom	Sum of squares	Mean sum of squares	F
Factor A	$a - 1$	$SSA = bn \sum_{i=1}^a (\bar{Y}_{i..} - \bar{Y}_{...})^2$	$MSA = \frac{SSA}{a - 1}$	$\frac{MSA}{MSE}$
Factor B	$b - 1$	$SSB = an \sum_{j=1}^b (\bar{Y}_{.j.} - \bar{Y}_{...})^2$	$MSB = \frac{SSB}{B - 1}$	$\frac{MSB}{MSE}$
Interaction	$(a - 1)(b - 1)$	$SSAB = n \sum_{i=1}^a \sum_{j=1}^b (\bar{Y}_{ij.} - \bar{Y}_{i..} - \bar{Y}_{.j.} + \bar{Y}_{...})^2$	$MSAB = \frac{SSAB}{(a - 1)(b - 1)}$	$\frac{MSAB}{MSE}$
Error	$ab(n - 1)$	$SSE = \sum_{i=1}^m \sum_{j=1}^n (Y_{ij} - \bar{Y}_{i.} - \bar{Y}_{.j} + \bar{Y}_{..})^2$	$MSE = \frac{SSE}{ab(n - 1)}$	
Total	$abn - 1$	$SSTO = \sum_{i=1}^a \sum_{j=1}^b \sum_{k=1}^n (Y_{ijk} - \bar{Y}_{...})^2$		

Longitudinal

Source	Degrees of freedom	Sum of squares	Mean sum of squares	Expected sum of squares
Subject	$m - 1$	$SSS = n \sum_{i=1}^m (\bar{Y}_i - \bar{Y}_{..})^2$	$MSS = \frac{SSS}{m - 1}$	$\sigma^2 + n\sigma_\pi^2$
Time	$n - 1$	$SST = m \sum_{j=1}^n (\bar{Y}_{.j} - \bar{Y}_{..})^2$	$MST = \frac{SST}{n - 1}$	$\sigma^2 + m \sum_{j=1}^n (\mu_j - \mu_{..})^2$
Error	$(m - 1)(n - 1)$	$SSE = \sum_{i=1}^m \sum_{j=1}^n (Y_{ij} - \bar{Y}_i - \bar{Y}_{.j} + \bar{Y}_{..})^2$	$MSE = \frac{SSE}{(m - 1)(n - 1)}$	σ^2
Total	$mn - 1$	$SSTO = \sum_{i=1}^m \sum_{j=1}^n (Y_{ij} - \bar{Y}_{..})^2$		