## The Diamond of Integrability

I shall review recent progress in understanding the connections between representation theory, enumerative geometry, and integrable systems inspired by a certain class of physical theories (so-called  $N=2^*$  theories). Conveniently one can arrange most of known results into the Diamond https://math.berkeley.edu/~pkoroteev/diamond33.pdf. I will describe some of its corners as well as highlight open questions.